



SPACE TRIPS SUMMER SCHOOL



Theme 9: SPACE

Riga Latvia
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HALL THRUSTERS FOR SATELLITE PROPULSION

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Outline

1. Electric Propulsion & Hall Thrusters

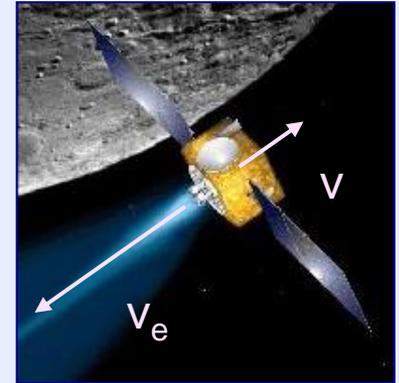
- Electric propulsion
- Principle of Hall Effect Thrusters

2. Research on Hall thrusters

- Simulation and plasma diagnostics
- Physics and technical issues
- Examples of recent achievements in France

3. Conclusion

- **Total velocity increment Δv** required for a given mission or manoeuvre is an indication of the energetic difficulty of that mission or operation



- **Momentum conservation** for a spacecraft $\frac{d[mv]}{dt} = 0$

$$m \frac{dv}{dt} = -v_e \frac{dm}{dt}$$

time varying mass of the vehicle → m $\frac{dv}{dt}$ → *acceleration of the vehicle*
 $-v_e$ → *velocity of the exhaust stream* $\frac{dm}{dt}$ → *rate of change of spacecraft mass due to propellant expulsion*

- Integration of this equation gives the propellant mass needed for a given velocity increment (i.e. for a given mission)

- **Electric propulsion** can provide large exhaust velocity of the propellant (acceleration of the propellant by electric force) but generally with small thrust
→ *adapted to satellite station keeping or interplanetary missions*
- **Chemical propulsion** provides small exhaust velocity (thermal expansion of the propellant) but large thrust is possible
→ *adapted to fast orbit transfer*

- **Specific Impulse** is a measure of the propellant velocity

$$I_{sp} = \frac{v_e}{g}$$

- **Thrust** is a measure of the force exerted on the satellite

$$T = v_e \frac{dm}{dt}$$

$$m \frac{dv}{dt} = -v_e \frac{dm}{dt}$$

- Integration over the whole duration of the mission

$$\frac{m_D}{m_0} = \exp \left[-\frac{\Delta v}{v_e} \right]$$

m_D = delivered mass

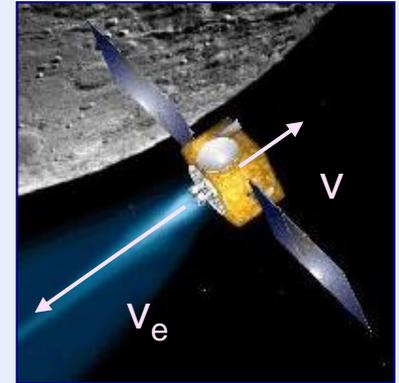
m_0 = initial mass = delivered mass + propellant mass = $m_D + m_P$

Δv = total velocity increment needed for the mission

$$\frac{m_D}{m_D + m_P} = \exp \left[-\frac{\Delta v}{v_e} \right]$$

$$\frac{m_P}{m_D} = \exp \left[\frac{\Delta v}{v_e} \right] - 1$$

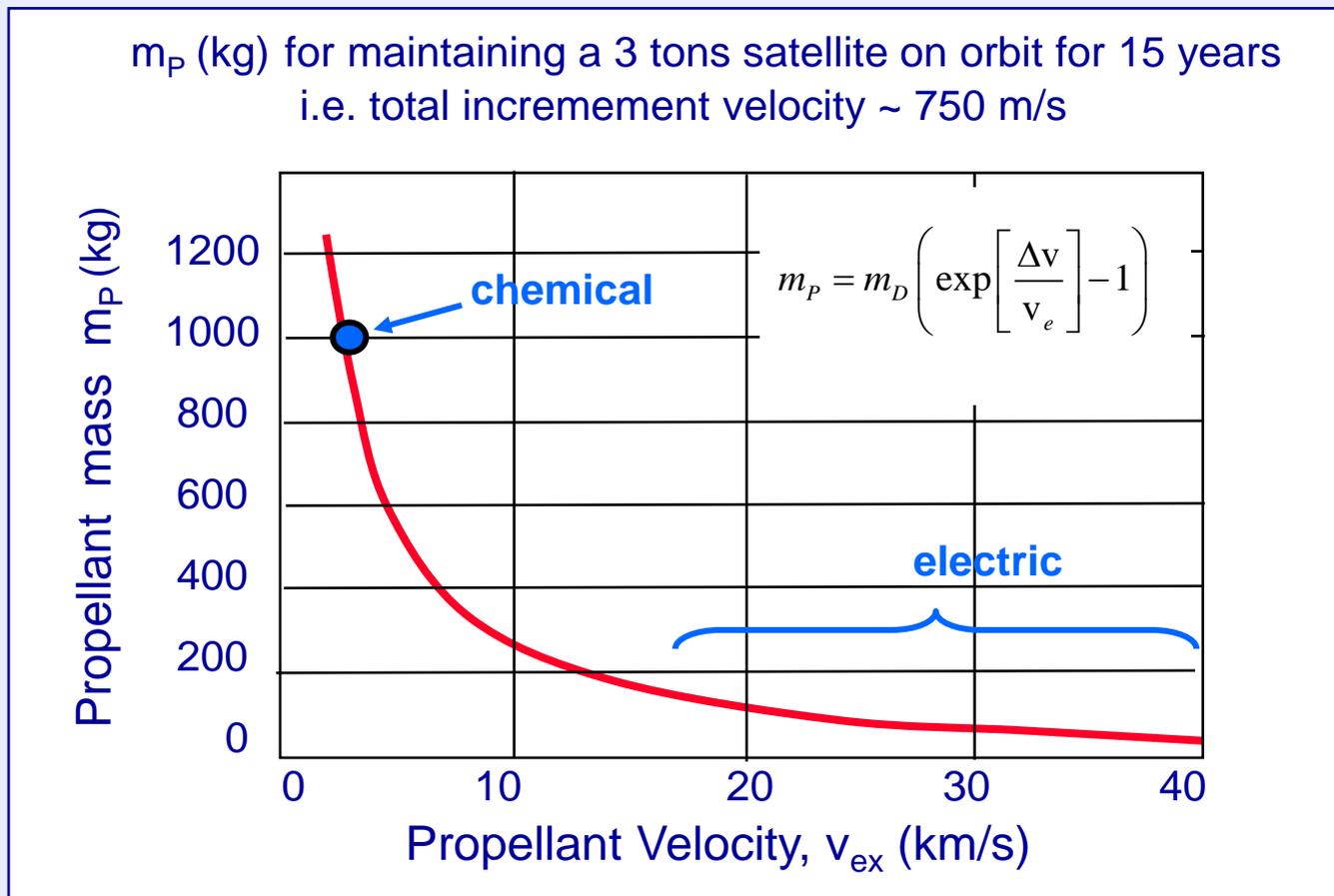
For a given total velocity increment of the vehicle, propellant mass consumption is smaller for larger propellant exhaust velocity



Electric Propulsion and Hall Thrusters

Propellant Consumption – Electric vs Chemical Propulsion

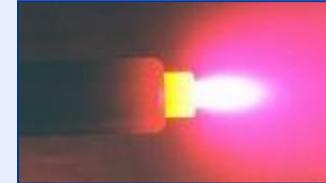
- Propellant mass consumption decreases exponentially with propellant exhaust velocity
 - High propellant velocity can be reached with electric thrusters
 - Electric propulsion saves more than 800 kg of propellant to keep a 3 tons satellite on geo orbit
- Cost reduction of millions of Euros



➤ **Electrothermal**

Gas heating + expansion

Arc Jet, resistojet, microwave

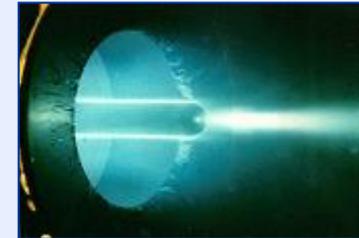


➤ **Electromagnetic** (MPD, MagnetoPlasmaDynamic)

Plasma acceleration by Lorentz force + expansion

Pulsed Plasma Thruster

Lorentz Force Accelerator



➤ **Electrostatic** (Ion thrusters)

Plasma source + ion extraction

Gridded ion thruster

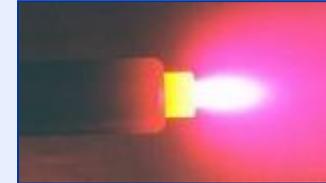
Field Emission Electric Thruster



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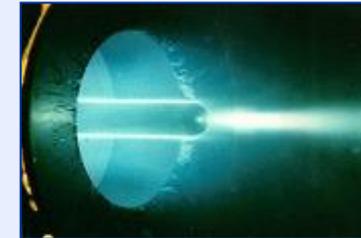


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Lorentz Force Accelerator



Hall Effect Thruster →

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Plasma source + ion extraction

Gridded ion thruster

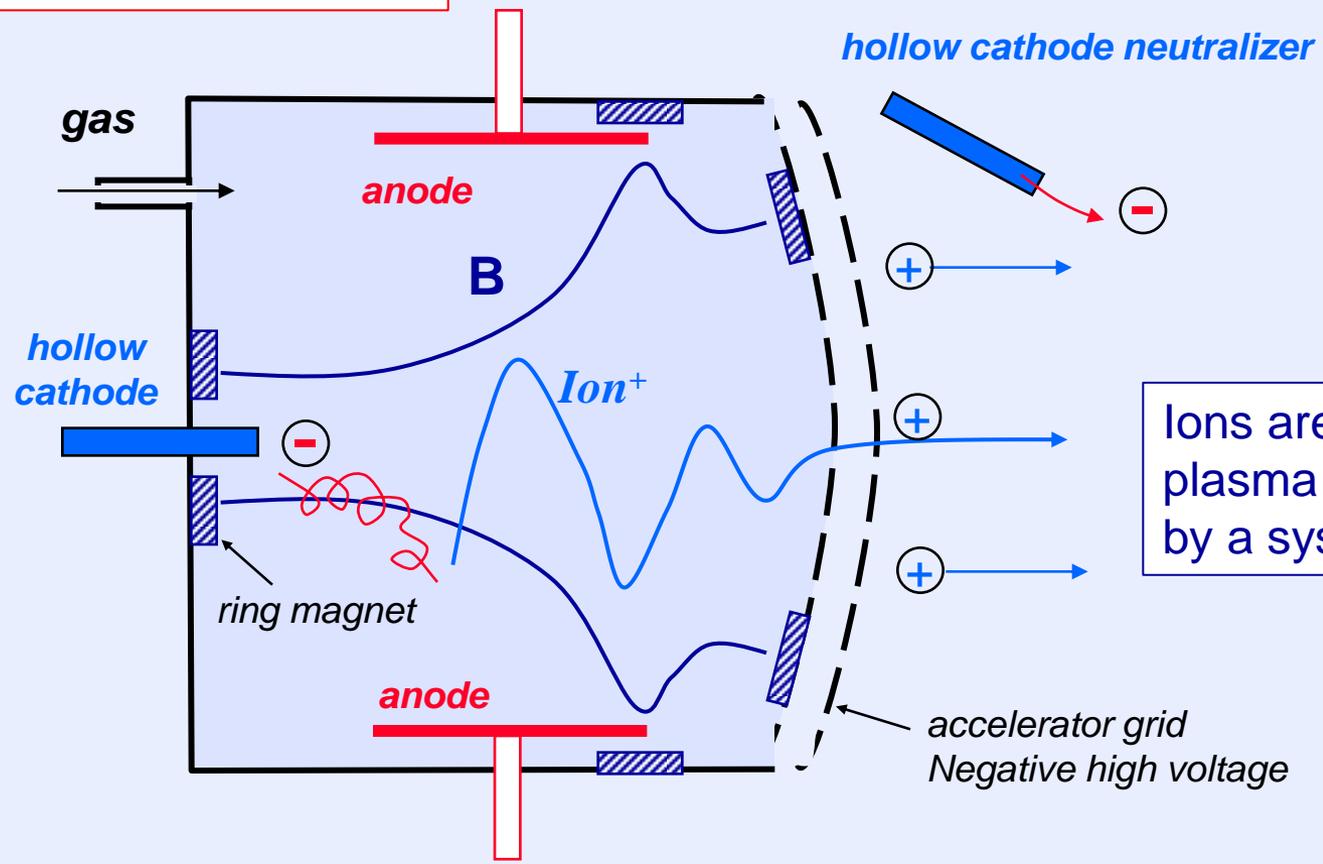
Field Emission Electric Thruster



- Plasma = ionized gas
- Contains gas molecules, free electrons and positive ions with densities n_g , n_e and n_i
- In a plasma n_e and n_i must be sufficiently large to have **quasi-neutrality** $n=n_e \sim n_i$
(non-neutrality generate electric fields and forces that keep negative and positive charges together)
- If plasma density n is large enough plasma can be a **good conductor**
 - Plasma tends to be equipotential (low electric field in plasma)
- Plasma is sustained by **ionization** by electron impact of the molecules
- Ionization must be sufficient to compensate for the charged particle losses (eg to the walls)
- To increase ionization electron energy must be increased
- Electron energy is increased by applying external field (DC, AC, microwave, etc...)
- At very low pressure, eg 1 Pa, the electron mean free path (distance between collisions with the molecules) can be larger than the dimensions of the plasma source
 - Ionization of the molecules is difficult (no collisions)
 - Magnetic field generally used to confine the electrons at low pressure

Gridded Ion Sources

Gridded Ion Thruster



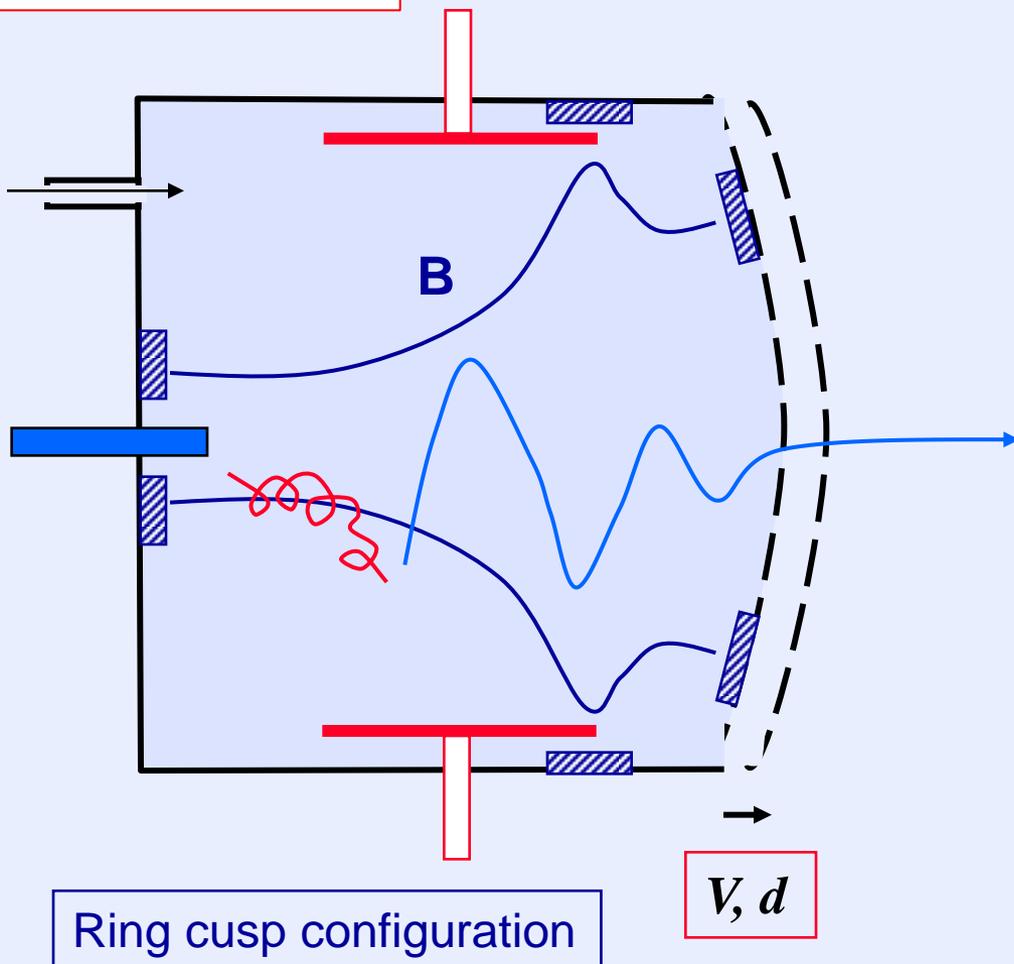
Ions are extracted from the plasma and accelerated out by a system of biased grids

Ring cusp configuration

- cathode : hot filament or hollow cathode
- magnetic confinement
- ~100 V between cathode and anode

Gridded Ion Sources

Gridded Ion Thruster



Ion current density limited by Child Langmuir law

$$j_i = \frac{4\epsilon_0}{9} \left(\frac{2e}{m_i} \right)^{1/2} \frac{V^{3/2}}{d^2}$$

Xenon, 1 kV, 1 mm $\rightarrow j_i = 0.01 \text{ A/cm}^2$
 - to get an ion current of 6 A
 - need an extracting area of 600 cm²
 i.e. 30 cm diameter

few 10s mA/cm²

Maximum Thrust/Unit Surface

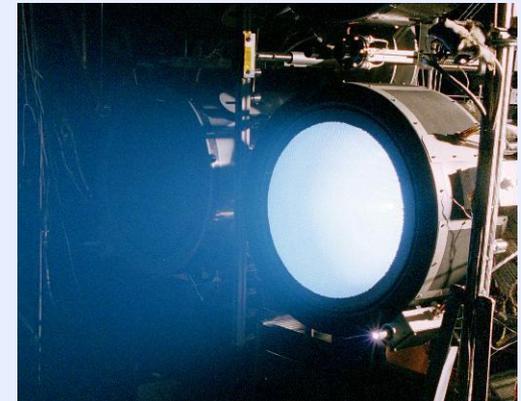
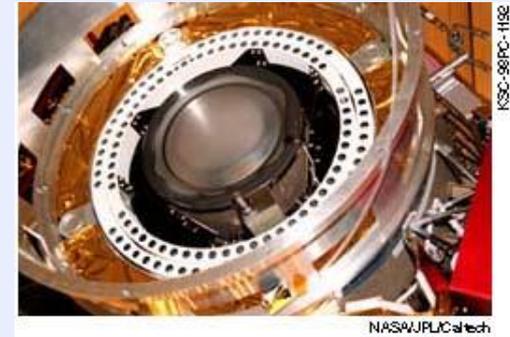
$$\frac{T}{A} = \frac{\dot{m}_i v}{A} = \frac{m_i}{e} j_i v \quad v = \sqrt{\frac{2e}{m_i} V}$$

$$\frac{T}{A} = \frac{8}{9} \epsilon_0 \left(\frac{V}{d} \right)^2$$

few N/m²

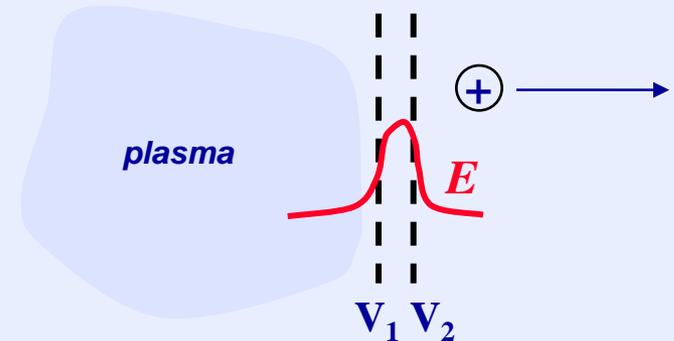
➤ Examples of gridded ion thruster

- **NSTAR**: used on the NASA Deep Space 1 mission (1998)
30 cm diameter, $P=2.3$ kW, $I_{sp}=3100$ s, $T=20-90$ mN
- **NEXT: NASA Evolutionary Xenon Thruster**
40 cm diameter, $P=1-6$ kW, $I_{sp}=2000-4000$ s, $T=50-240$ mN



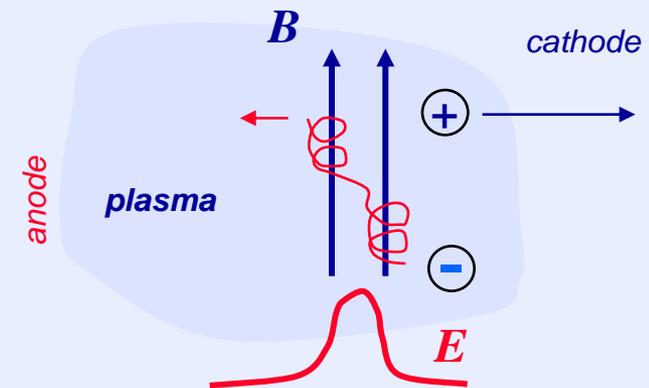
➤ Gridded ion source

- Space charge limited current density (Child Langmuir)
Large thrust → large thruster area
- Sputtering limits the life time of the grids



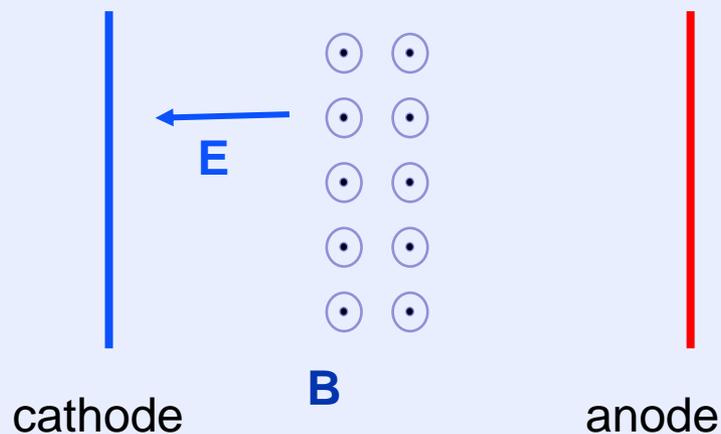
➤ Gridless ion source – Hall Thruster

- Large electric field generated in the plasma
- How to create large electric field in the plasma ?
- Decrease electron conductivity locally $E = \frac{J}{\sigma}$
- Can be done by perpendicular magnetic field
« **magnetic field barrier** »
- No limitation on current density



Gridded and Gridless ion source

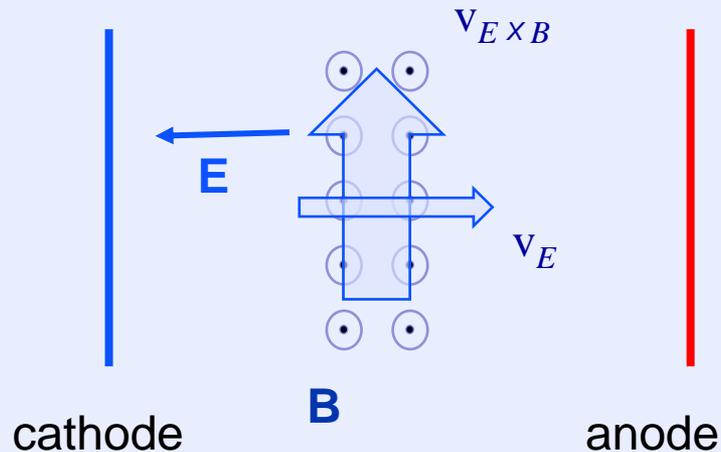
- **Magnetic barrier between cathode and anode in a plasma source**
 - Perpendicular to electron flow from cathode to anode
 - Increase electron residence time and ionization
 - Ions are ~ not magnetized (not sensitive to magnetic field because of large mass)



- Electron drift // to \mathbf{E} is considerably reduced
- Electron drift in the $\mathbf{E} \times \mathbf{B}$ direction with large velocity (Hall current)

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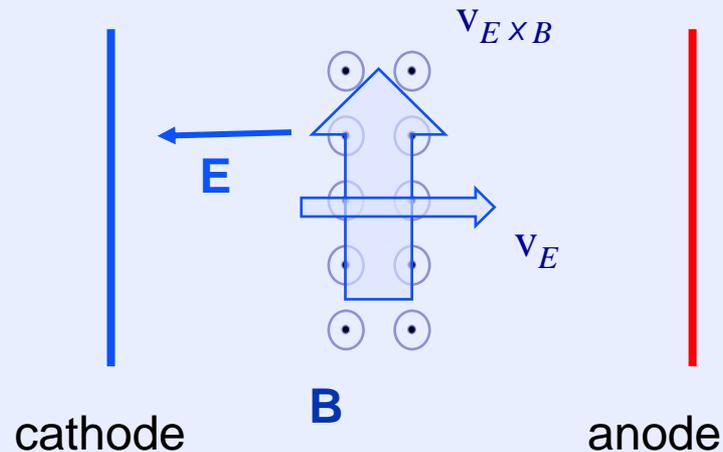
$$E \times B \text{ drift velocity: } v_{E \times B} = E/B$$

$$E \text{ drift velocity: } v_E = E/B \nu/\omega$$

ν electron collision frequency
 ω electron cyclotron frequency = eB/m
 ν/ω can be $\sim 10^{-3}$ in a Hall thruster

Gridded and Gridless ion source

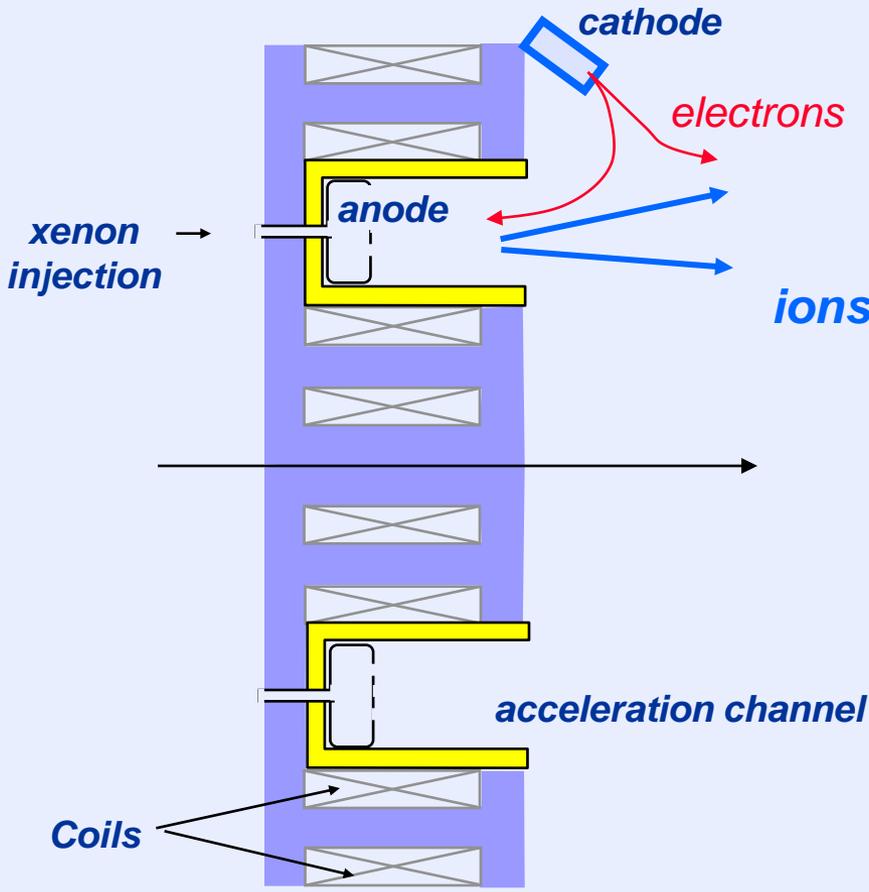
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$E \times B$ drift velocity: $v_{E \times B} = E/B$
 E drift velocity: $v_E = E/B \nu/\omega$

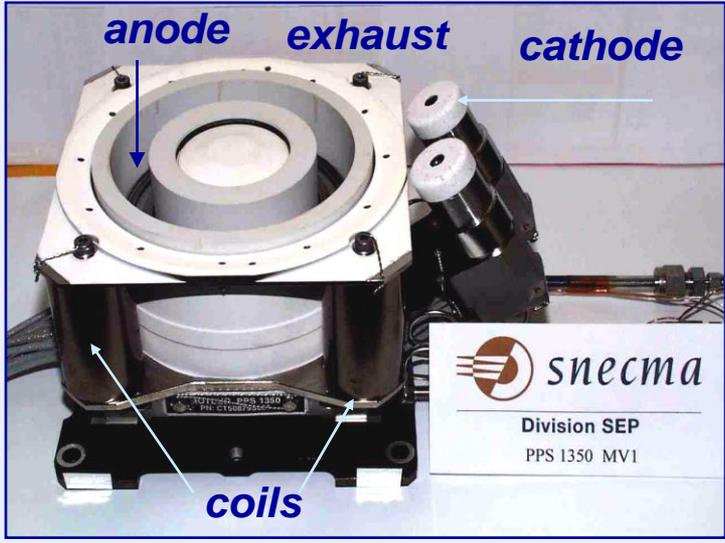
- Because of electron flux in the $E \times B$ direction, there should be no walls in this direction
- Closed drift geometry (i.e. cylindrical with $E \times B$ in the azimuthal direction)
- Hall thrusters

Hall thruster

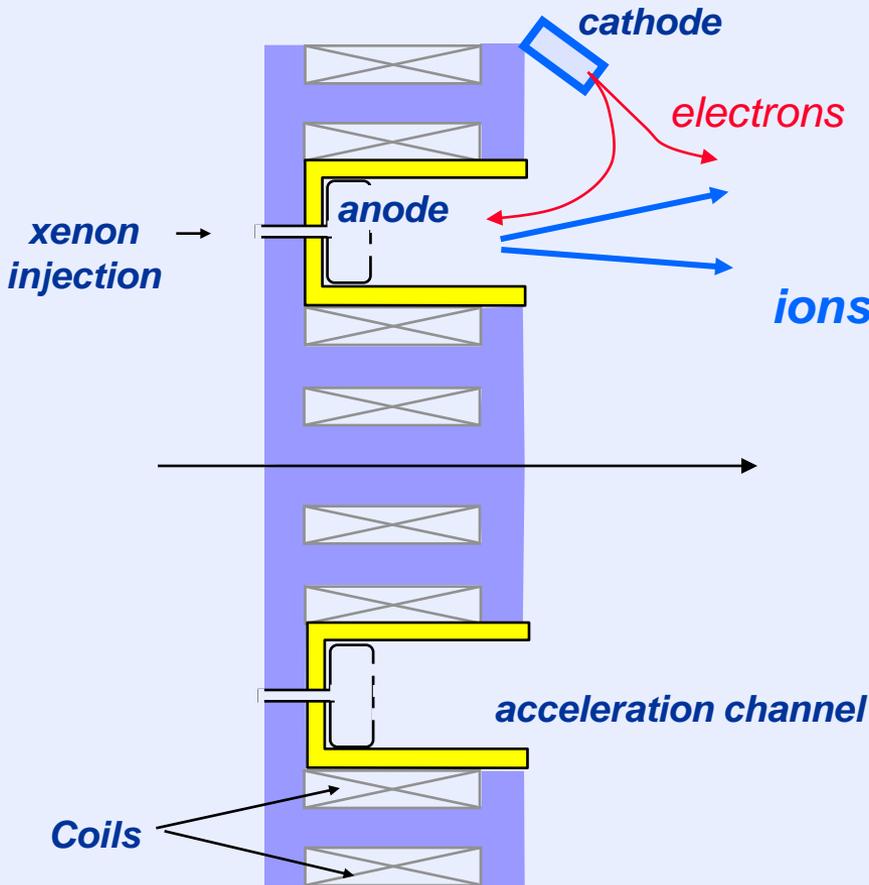


- High Thrust Efficiency > 50 %
- High propellant velocity ~20 km/s
- Thrust to Power Ratio ~ 70 mN/kW

$E \times B$ drift in the azimuthal direction

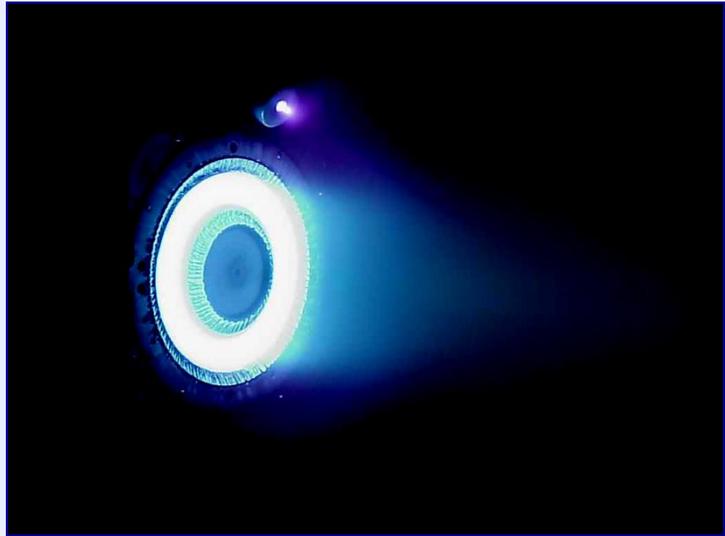


Hall thruster



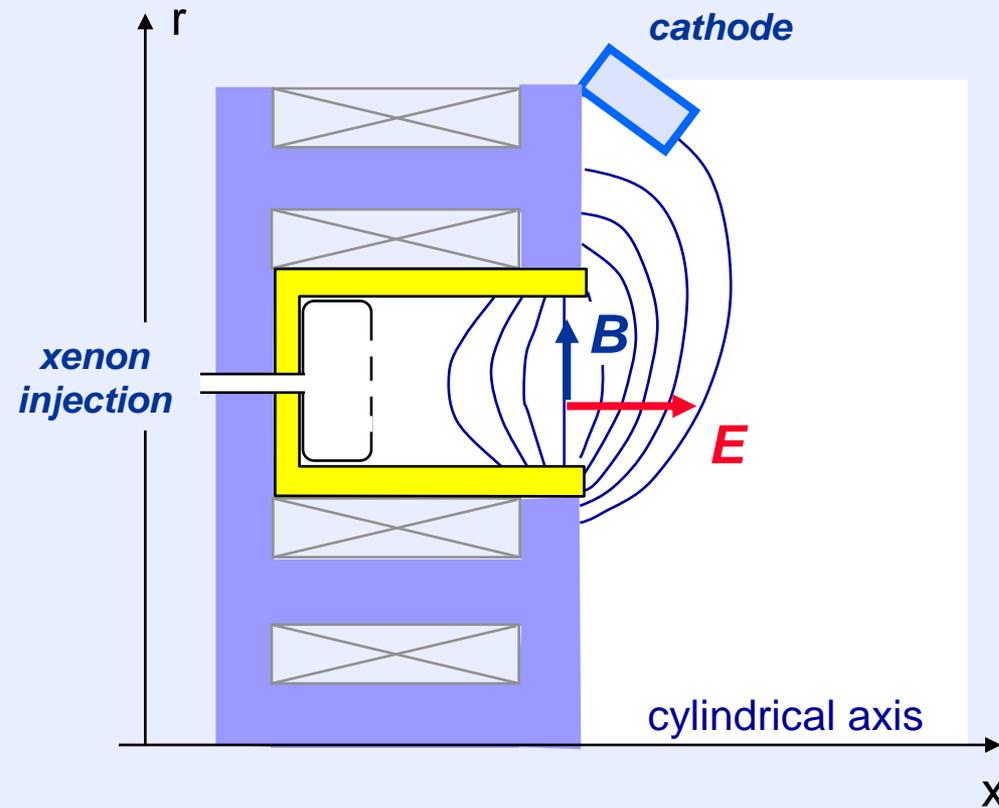
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$E \times B$ drift in the azimuthal direction



European lunar probe SMART 1

Hall thruster



Principles

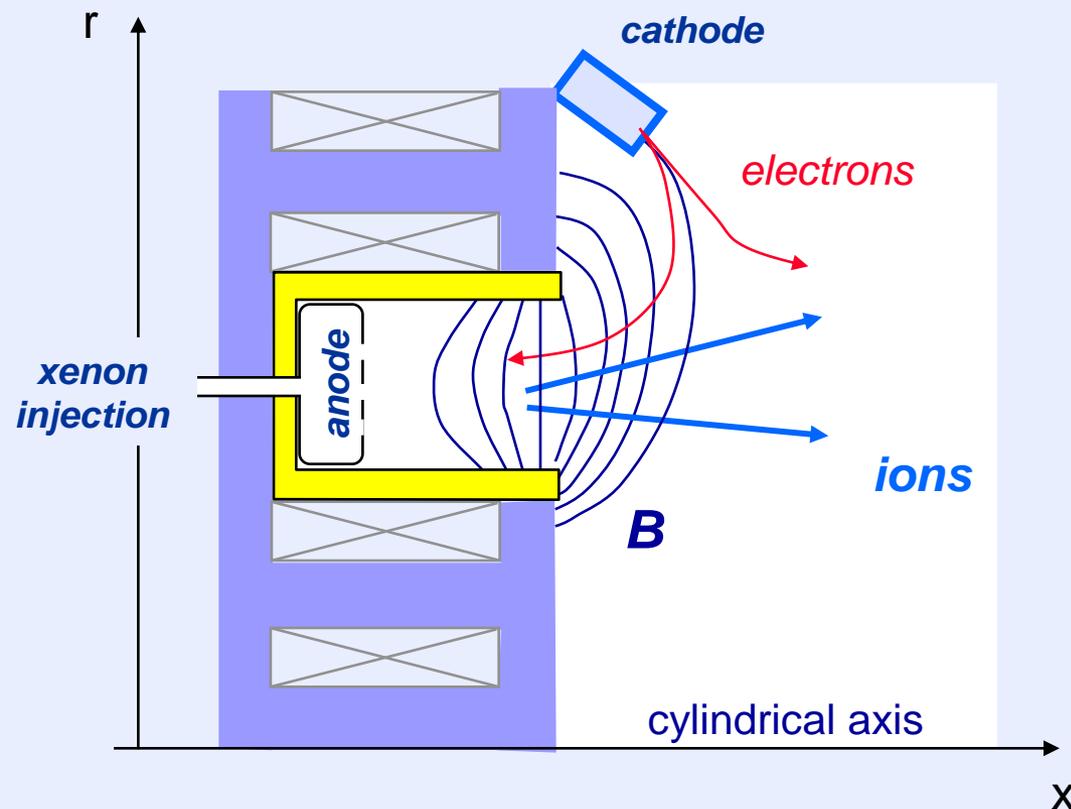
- Radial magnetic field B
- Axial electric field E
- $E \times B$ drift in the azimuthal direction

- Existence of large electric field in the plasma because of low electron conductivity in the magnetic barrier:

$$J = \sigma E$$

If conductivity σ is low, electric field $E = J/\sigma$ must increase for a given current

Hall thruster



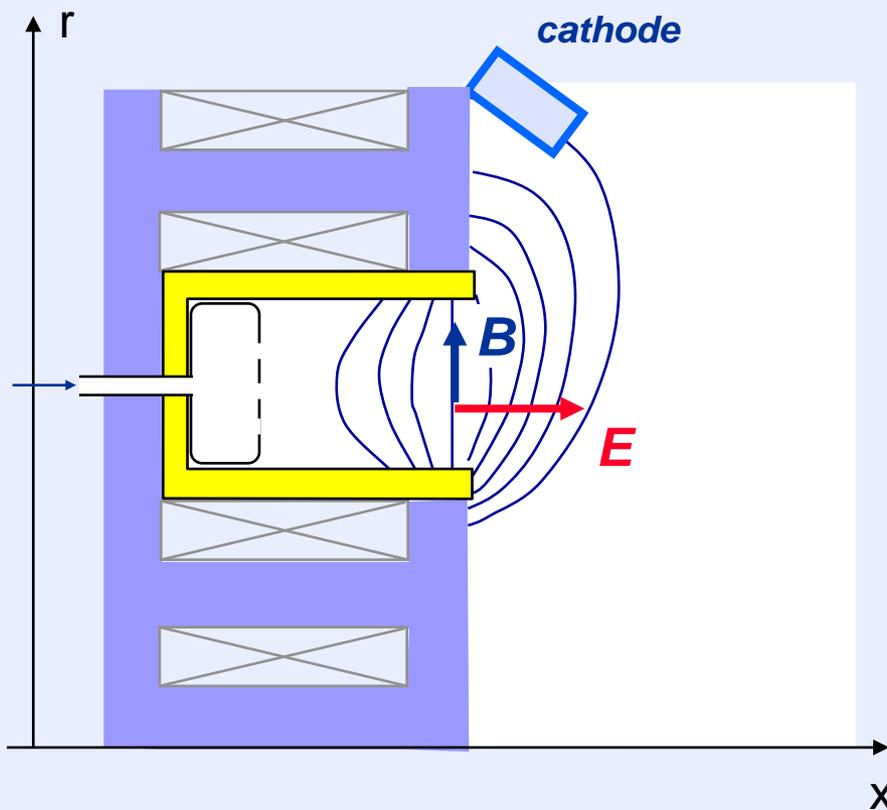
Principles

- Mean free paths \gg dimensions
- Large radial B field at exhaust ($2 \cdot 10^{-2}$ T)
 - increase residence time of electrons
 - **Magnetized, collisional electrons**
- **Unmagnetized, Collisionless ions**
- Neutral flow \sim fully ionized (80-90%)

Typical numbers

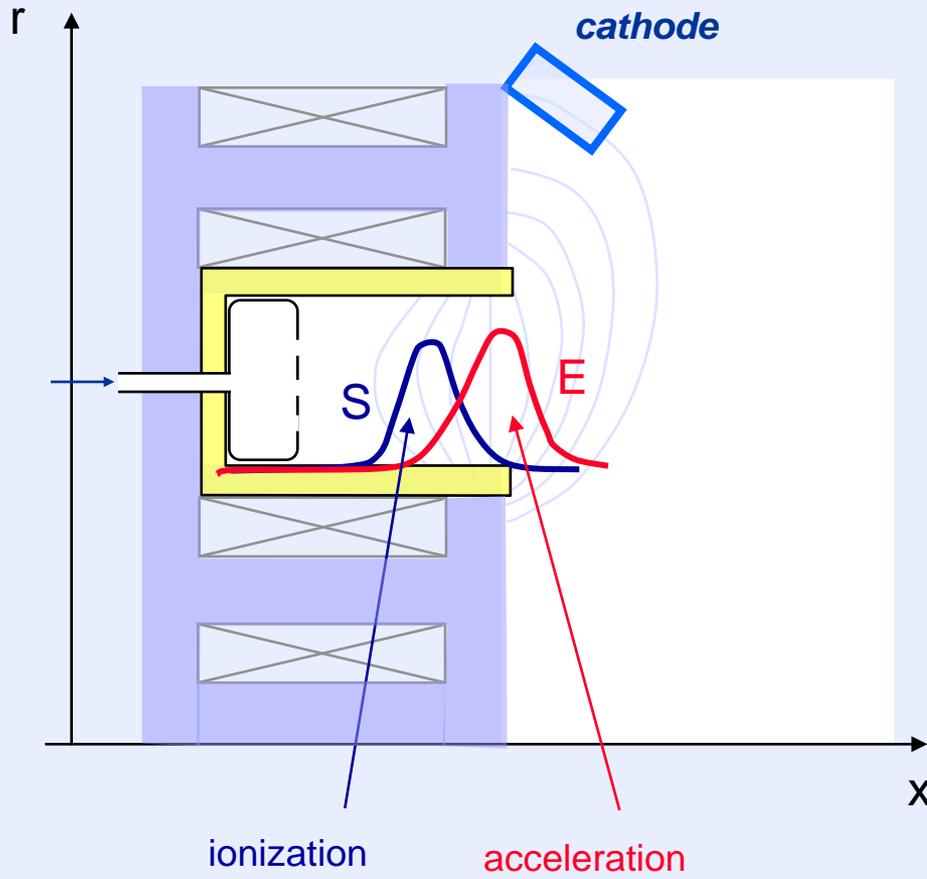
- Voltage **300 V**, current **4 A**
- Xenon mass flow rate 5 mg/s
- Typical dimensions ϕ 10 cm, L 3 cm
- gas density at anode 10^{13-14} cm $^{-3}$
- Plasma density 10^{12} cm $^{-3}$
- Electron temperature 15 eV

$E \times B$ configuration \rightarrow **Hall (azimutal) current** ~ 20 A , larger than the discharge current ~ 4 A



Two ways to describe thrust

- Electric force acting on ions and due to the large electric field generated by the decrease of electron conductivity
- Lorentz force acting on the Hall current

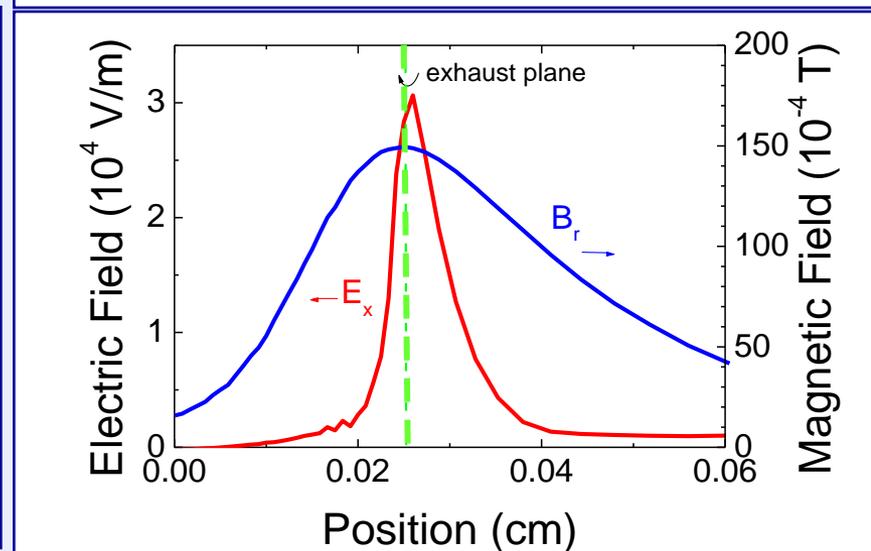
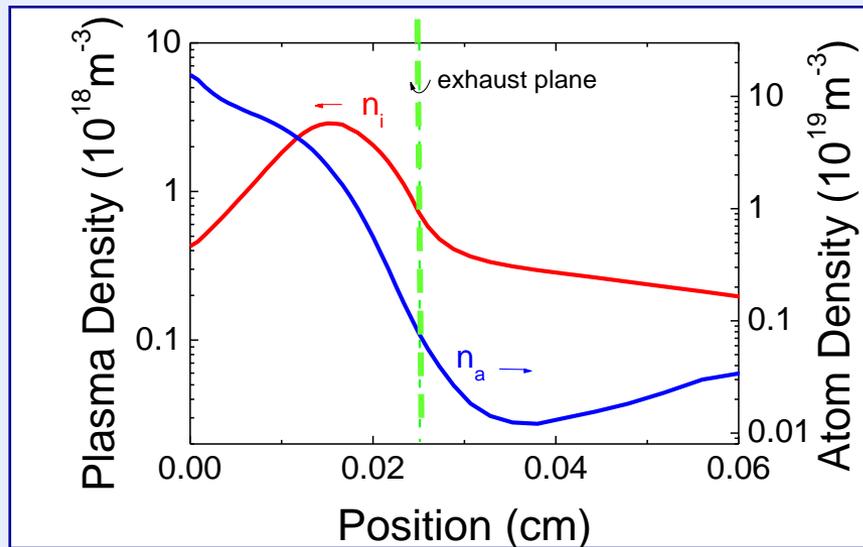
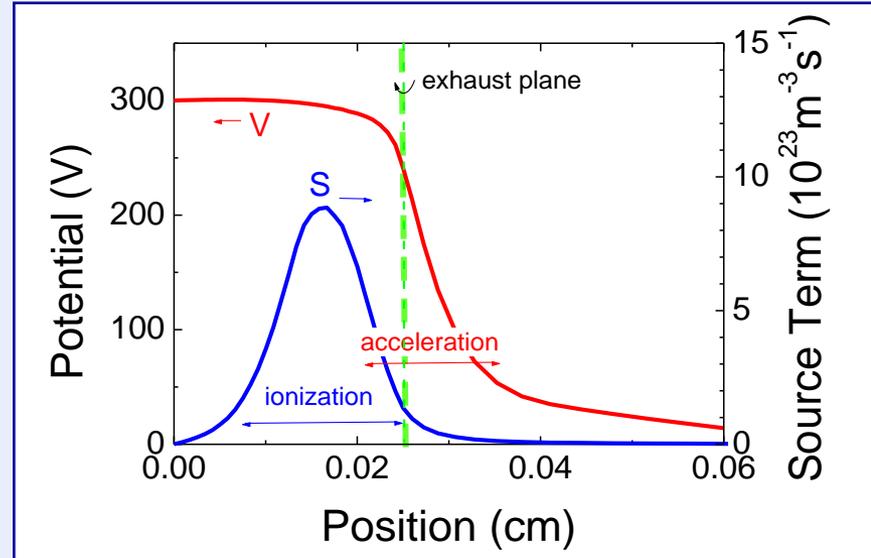
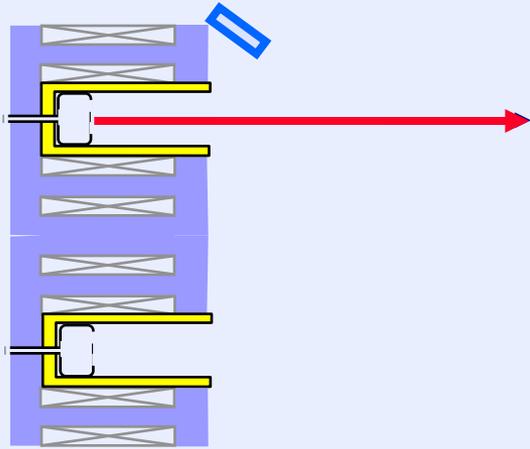


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graph TD; A[radial B field] --> B[trapped electrons]; B --> C[low axial electron conductivity]; C --> D[large axial electric field]; D --> E[enhanced ionization]; E --> F[ION ACCELERATION]; B --> E;
```

A flowchart illustrating the operational principles of a Hall thruster. It starts with a 'radial B field' which leads to 'trapped electrons'. This results in 'low axial electron conductivity', which in turn creates a 'large axial electric field'. This field leads to 'enhanced ionization', which finally results in 'ION ACCELERATION'.

Research on Hall thrusters

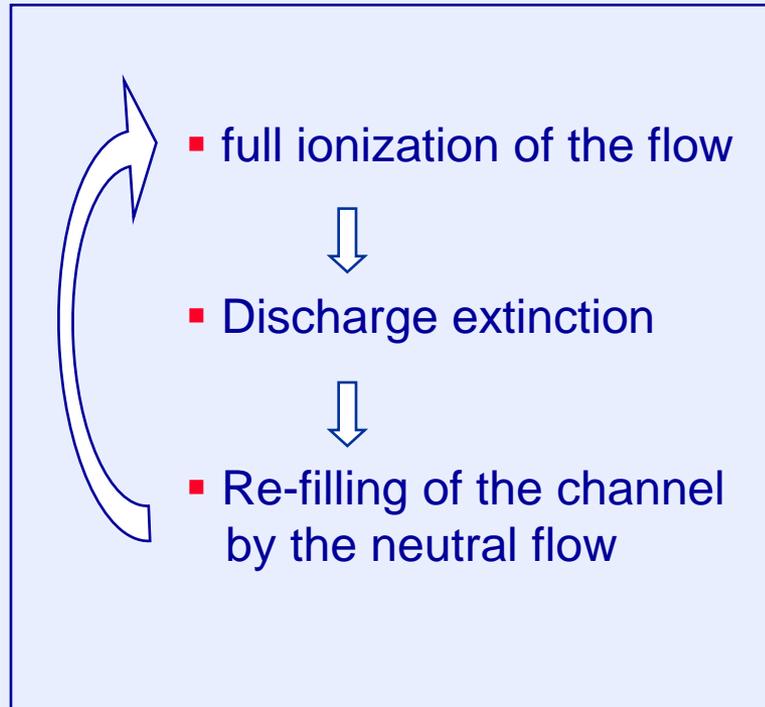
Typical plasma properties from 2D Hybrid model



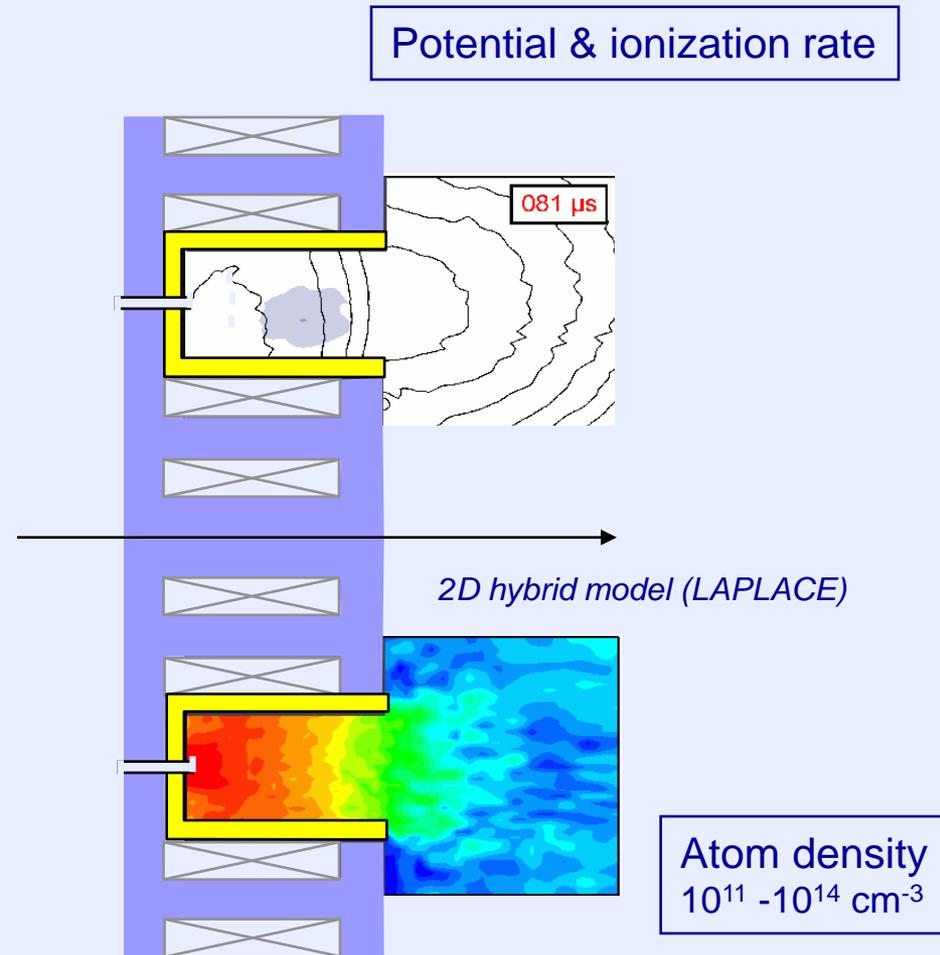
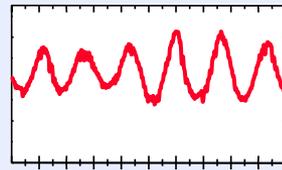
Hybrid model: fluid description of electrons, kinetic description of ions

Research on Hall thrusters

Hybrid model predictions – Neutral density and current oscillations



large amplitude (few A)
low frequency (10 kHz)
current oscillations



Bareilles et al. Phys. Plasma 11, 3035 (2004)

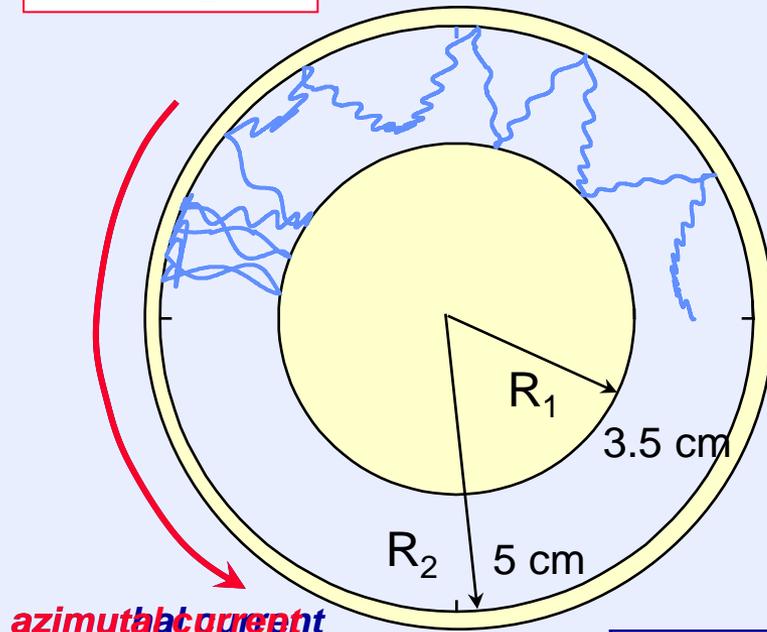
Research on Hall thrusters

Classical, collisional transport – Axial and azimuthal velocity

Azimuthal electron current (Hall current)= 20 A

Axial electron current at channel entrance= 1A

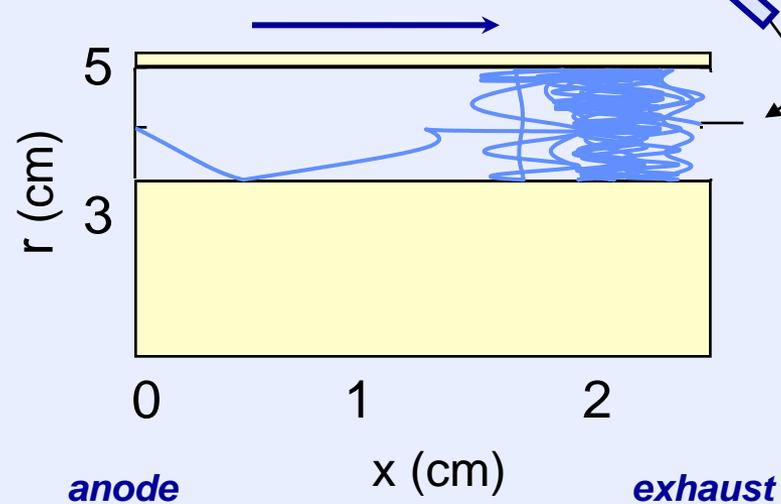
$$v_{E \times B} = \frac{E}{B}$$



$$v_E = \frac{E}{B} \frac{v}{\omega}$$

$$\omega = \frac{eB}{m}$$

Axial current



Classical electron conductivity across B

- Axial velocity proportionnal to collision frequency i.e. to **gas density**
- No collisions → no « classical » axial transport

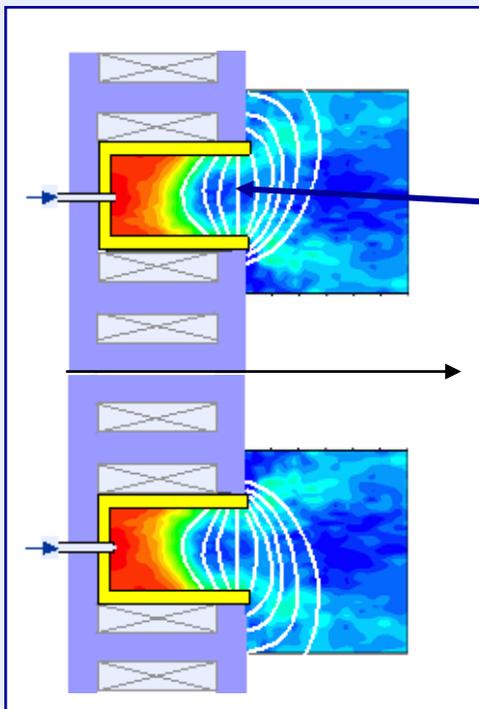
- **In classical theory electron current is proportional to electron-neutral collision frequency, i.e. to gas density**

$$v_E = \frac{E}{B} \frac{\nu}{\omega} \quad \text{electron current density} \quad J_e = en_e v_E = en_e \frac{E}{B} \frac{\nu}{\omega}$$

- **Problem**

- experiments and models show that classical conductivity is not sufficient to explain observations
- i.e. current density due to collisions between electrons and neutral gas is too low

Neutral atom density

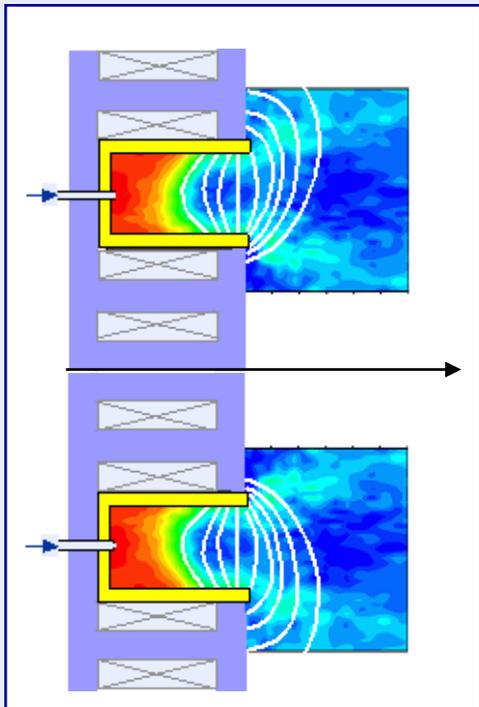


- Because of ionization, neutral density is depleted in the exhaust region
 - Collisions with neutral atoms not sufficient to allow transport $\perp B$ (especially outside the channel)
- Necessary to introduce supplementary scattering effects in hybrid models (« anomalous mobility »)
 - **Collisions with walls and secondary emission (« near wall conductivity »)**
 - **Turbulent transport**

Adam et al. Plasma Physics and Controlled Fusion 50 124041 (2008)

Research on Hall thrusters

Physics Issue: Classical and anomalous conductivity



- Research efforts to understand and quantify electron transport across magnetic field
 - Particle In Cell simulation of turbulence
 - Possible to deduce turbulent transport coefficients for fluid models ?
 - Plasma diagnostics to measure plasma properties and quantify turbulence: Laser diagnostics (Laser Induced Fluorescence, Collective Thomson Scattering)

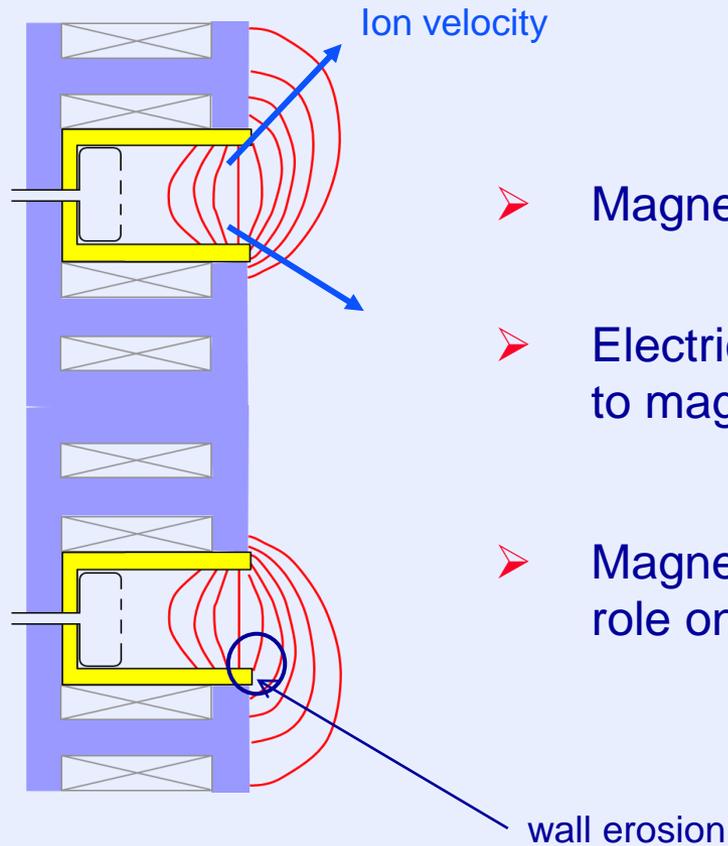
- Because of anomalous transport, the models are still not able to help efficiently the design of new Hall thrusters (larger power or different designs):

Hall thruster design is still empirical

Adam et al. Plasma Physics and Controlled Fusion 50 124041 (2008)

Research on Hall thrusters

Other Issue: Ion divergence and wall erosion

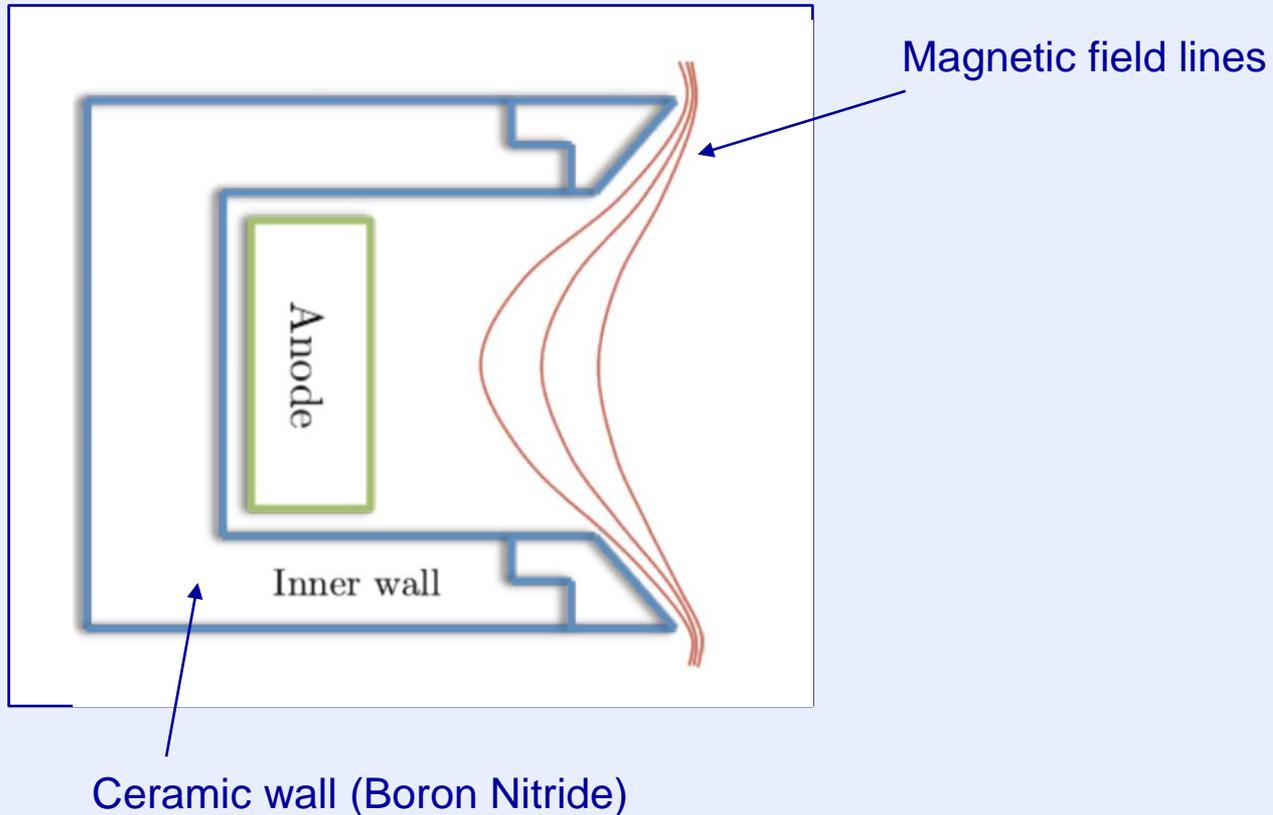


- Magnetic field lines tend to be equipotential
- Electric field and ion trajectories ~ perpendicular to magnetic field lines
- Magnetic field configuration plays an important role on ion divergence and wall erosion

Research on Hall thrusters

Other Issue: Ion divergence and wall erosion

- Magnetic shielding configuration proposed by JPL to minimize wall erosion and increase lifetime



Hofer et al, IEPC-2013-033

Some important issues

- Better understand and quantify electron transport across magnetic field to build predictive simulation tools than can help the design of Hall thrusters
 - understand role of instabilities and turbulence on transport
 - understand role of electron interaction with walls on transport

- Understand the role of magnetic field distribution
 - on instabilities, turbulence and electron transport
 - on ion beam distribution and divergence – wall erosion – lifetime

- Improve materials
 - Development of new ceramic materials to increase lifetime

- Investigation of plasma surface interaction (eg secondary electron emission)

- Improve cathode (electron source)

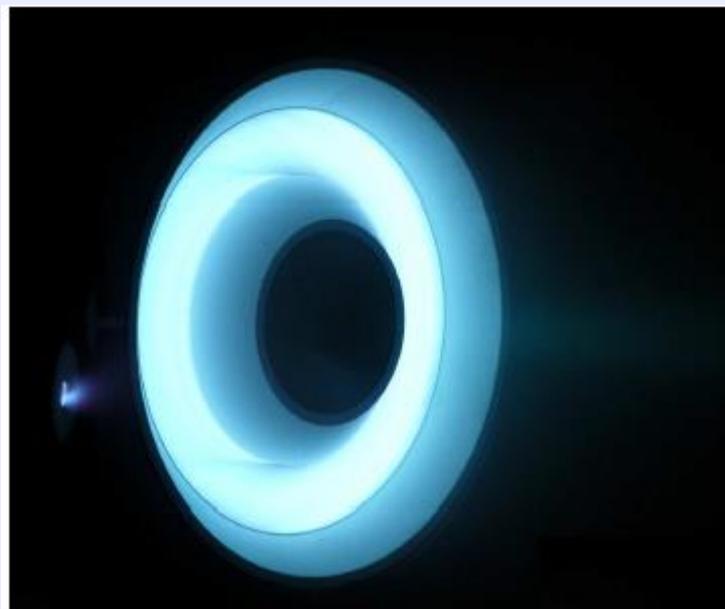
Research on Hall thrusters

Example of recent achievements

PPS FLEX

(French research group on electric propulsion)

- Design of a Hall thruster with Flexible magnetic field configuration: PPS FLEX
- Possible to test multiple magnetic field configurations on a single thruster
- Possible to change each parameter independantly (eg B gradient) to understand the role of each parameter on the thruster performance

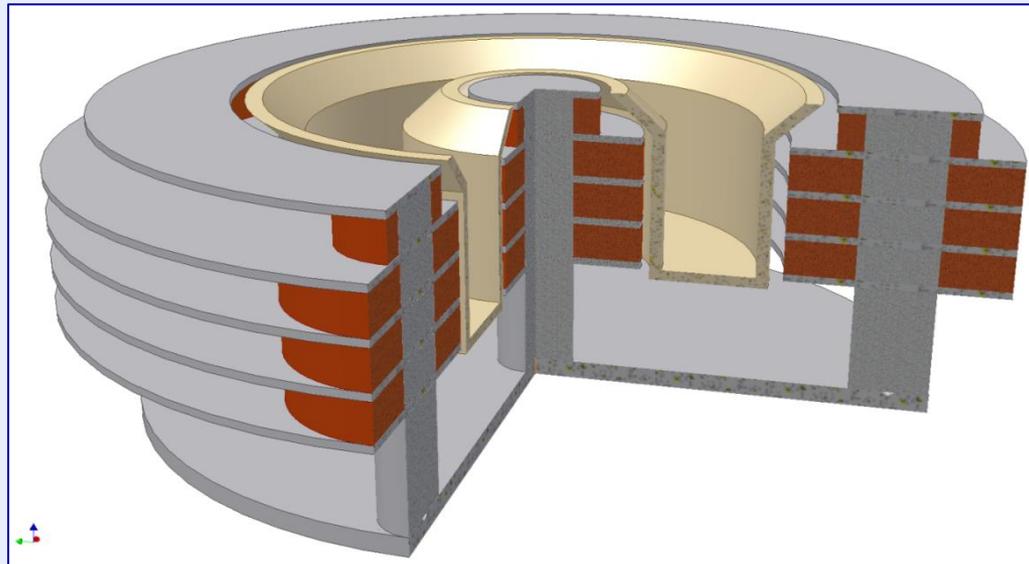


Hénaux et al, IEPC-2011-291

PPS FLEX

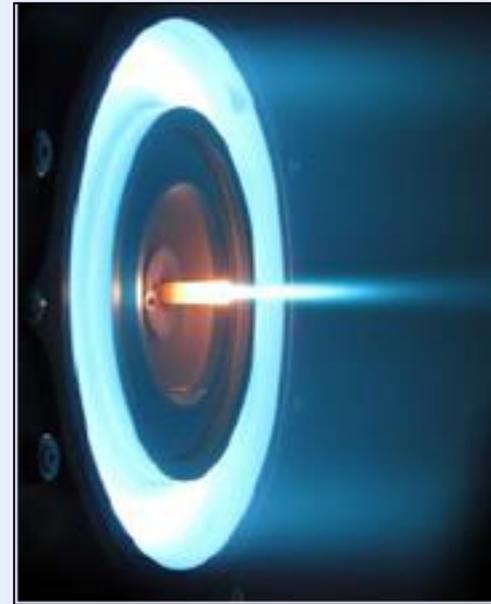
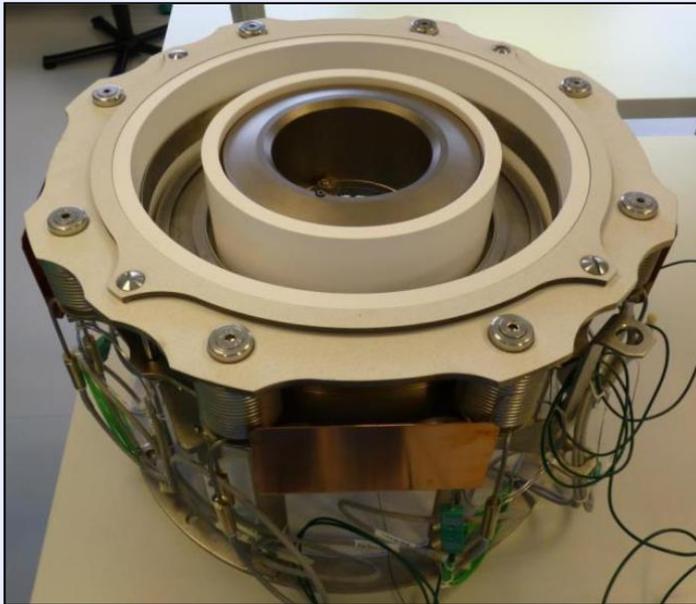
(French research group on electric propulsion)

- Complex system of independent coils and magnetic circuit
- 8 degrees of freedom



PPS-20k ML

(French research group on electric propulsion)

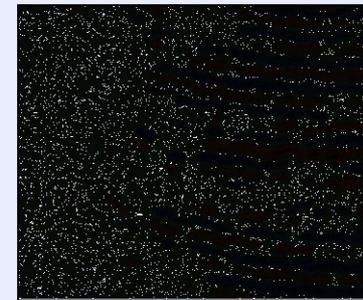


Hall effect thruster PPS-20k ML operating at 23.5 kW,
developed in the frame of the FP7 HiPER

Simulations and diagnostics

(French research group on electric propulsion)

- Evidence of the presence of azimuthal instabilities (microturbulence) enhancing electron transport across the magnetic field by Particle-In-Cell simulations
- Measure of density fluctuations and turbulence by Collective Thomson Scattering
- Laser Induced Fluorescence measurements of ion velocity distribution function

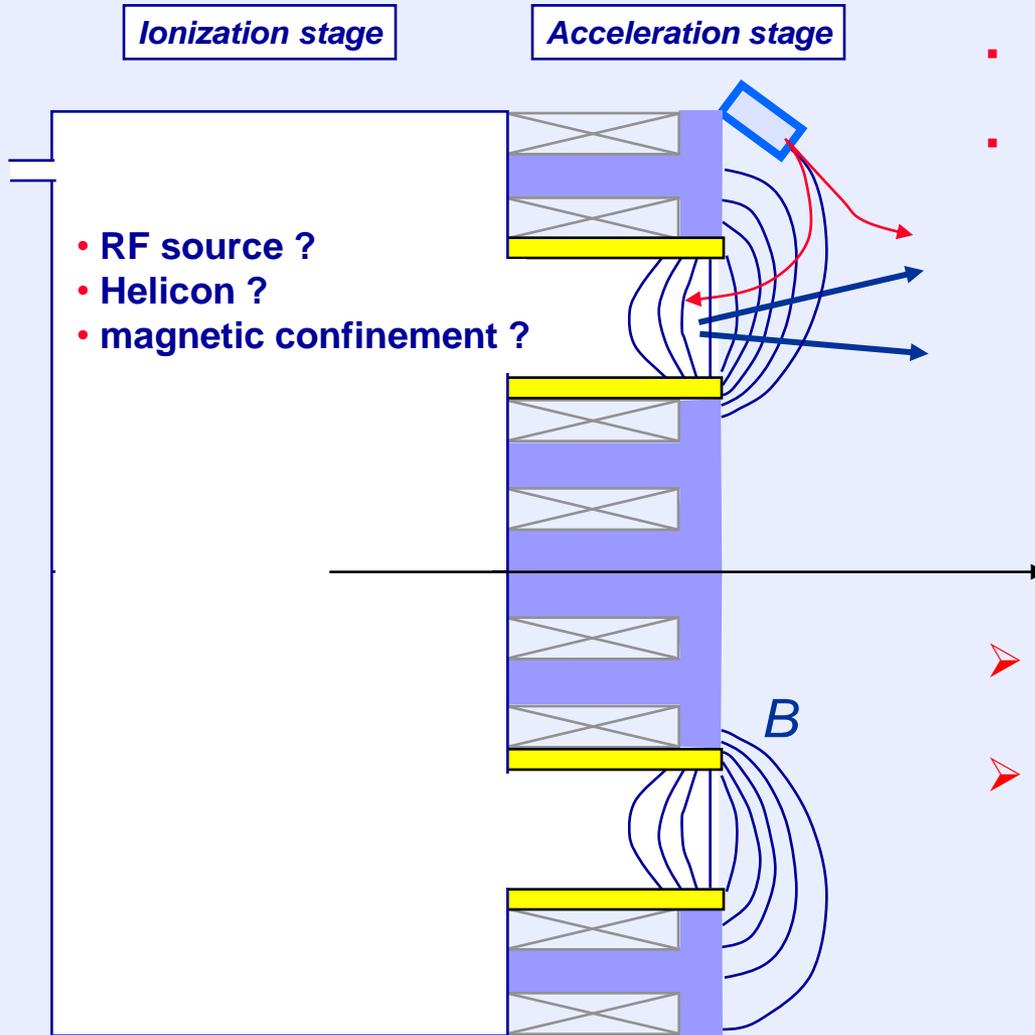


Need for more versatile Hall thrusters

- In a Hall thruster the same electric field is used to energize the electrons (allowing ionization) and to accelerate the ions
- ionization and acceleration are strongly linked so it is difficult to fix separately the power (thrust) and the ion velocity (I_{sp})
- **Need for versatile thrusters with variable I_{sp} and thrust**
 - orbit top up – orbit raising
 - high thrust (reduction of mission duration)
 - high mass flow rate/low voltage (enhance ionization)
 - North/South Station Keeping
 - high I_{sp} to minimise gas consumption
 - high voltage/low mass flow rate to enhance acceleration
- **Double Stage Hall Thruster (DSHT)**
 - Separation of ionization and acceleration processes
 - promising candidate for multi-mode operation

Research on Hall thrusters

Double Stage Hall Thruster



- **Ionization Stage**
Use a separate chamber for plasma generation
- **Acceleration Stage**
Acceleration in channel as in standard Hall thrusters

- Many attempts at developing DSHTs
- But results are not yet convincing in terms of performance and efficiency

Conclusion

- 1. Interest in all-electric propulsion is increasing fast**
- 2. EP will be used on all telecommunication satellites not only for station keeping but also for orbit raising**
- 3. Hall thrusters are excellent candidates for EP and are already used on satellites – Still need for Research and Development**
- 4. Principles of Hall thrusters are relatively simple but physics is quite complex**
 - Electron transport across magnetic field
 - Role of plasma-wall interactions
 - Design is still empirical
 - Important progress made in the last years on physics and technical issues